

# Multibody Dynamics A - wb1310

Lecture 3, course 2014-2015

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TU Delft, 3mE/BmechE



## Multibody Dynamics A wb1310 (fall 2014, Q2)

Instructor: [Arend L. Schwab](#)



MSC SOFTWARE

TU Delft

Delft University of Technology

**Description:** Multibody Dynamics A is an introductory course in applied dynamics of mechanical systems. The emphasis is on the usage of multibody dynamics software. We want you to learn enough about dynamics in 3D that you will be able to use a standard multibody dynamics software package correctly, appreciate the limitations, and say some sensible things about the model at hand.

In the course you will learn about the fundamentals of Multibody Dynamics: the description of the orientation of a rigid body in space, the Newton-Euler equations of motion for a 3D rigid body, how to add constraints to the equations of motion, and how to solve such a system of coupled equations. You will spend most of the time (80%) in doing the lab assignments. These assignments consist of a number of practical problems that have to be worked out with the software package ADAMS. Your findings are to be put down in a Lab Report.

**Goal:** By the end of the course you be able to make a complex model of realistic 3D mechanical system and draw some conclusions from the dynamical analysis.

**Grading:** The written exam is of the open book type and has the form of a questionnaire about the findings as written down in your lab report. The report serves as reference material for your exam. At the end of the exam the questionnaire together with the Lab Report are to be handed over. The final grading is 50% on the report and 50% on the written exam.

### News

#### Hand-Outs

- The course [Contents](#).
- The [Laboratory Assignments](#).
- A short [Introduction to ADAMS \(1,169 KB\)](#).
- Tire and Road files for assignment#5: [16r26\\_new.tir](#), [18r38\\_new.tir](#), [FlatRoad.rdf](#).

#### Office Hours

Instructor: Arend L. Schwab, [a.l.schwab@tudelft.nl](mailto:a.l.schwab@tudelft.nl), Monday, 15-17 h., room F-0-010, phone: 015 278 2701.  
TA: Sten Ponsioen, [s.l.ponsioen@tudelft.nl](mailto:s.l.ponsioen@tudelft.nl), Monday, 13-17 h. IO-PC hall 3 (SHIFT).

# Contents

| Lecture | Topic  | Assignment        |
|---------|--|-------------------|
| 1th-2nd | Introduction                                 | 1-Pendulum        |
| 1th-2nd | Newton-Euler eqn's of motion                 | 2-Wheel           |
| 3rd     | Modeling of Mechanical Systems               | 3-Crane           |
| 4th     | Orientation of rigid body in space           | 4-Governer        |
| 5th     | Coupled Differential And Algebraic Equations | 5-Tractor/Bicycle |
| 6th     | Overview                                     | 5-Tractor/Bicycle |

# Accounting

| Section                | Hours |
|------------------------|-------|
| Lectures               | 7*2   |
| Assignments (guided)   | 7*4   |
| Assignments (free)     | 7*4   |
| Class Prep             | 7*1   |
| ? <b>Written Exam!</b> | 7     |
| Total (3 ECTS)         | 84    |

Written exam: Thu 22 Jan 2015, 14-17 h.

## Assignment 3

In order to examine fast and correct positioning of a container on an Automated Guided Vehicle, we study the model of an overhead container crane (gantry crane). Here we only consider the motion of the crab plus container, the hoisting motion will not be considered. The cables in which the container hangs, are modelled as compliant spring-damper elements. The container measures 8x8x40 [ft] at a total mass of 30 [metric tons] (dead weight plus load). You may assume a uniformly distributed mass for the calculation of the mass moment of inertia quantities. The vertical distance between the bottom of the crab and the top of the container is 25 [m]. The supporting cables are modelled by 4 cables which are mounted on the container in a purely vertically centered way, with a distance of 2 [m] in transverse and 6 [m] in longitudinal direction between them. Each individual cable has a stiffness of  $3.0 \cdot 10^6$  [N/m] and a relative damping of 5 %. The driving motion of the crab is thought of as: first a constant acceleration, then a constant speed and finally a constant deceleration. The maximum speed is  $v_{max} = 240$  [m/min] and the maximum ac(de)celeration is  $a_{max} = 0.7$  [m/sec<sup>2</sup>]. A crane expert told us that for the load to hang still after the crab's driving motion, we have to accelerate and decelerate in a multiple of the Period of Vibration  $T$  of the load oscillation.

1. Make a pencil-and-paper estimate of the Period of Vibration  $T$  of the load oscillation in the crab's driving motion.

2. Determine the Period of Vibration of the load oscillation in the crab's driving motion of your ADAMS model, for instance by means of an eigenfrequency analysis (Simulation Control → Linear).
3. Simulate the motion of the container assuming a total displacement in the driving direction of the crab of 60 [m]. Check the statement of the crane expert, is he right? Plot the speed of the crab and the speed of the container in the crab's driving direction as a function of the *displacement* of the crab in the driving direction.

The crab motion can be generated by using a Translational Joint Motion. First create such a joint with a random value, after which the function  $F(\text{time})=$  can be modified in the Function Builder. By summation of a number of STEP functions you may obtain the desired motion.

4. As a rule, the container will be loaded asymmetrically and we are wondering what the effect of this will be on the container's positioning on the A.G.V. Assume the centre of mass to be 20 % = (1.6, 1.6, 8.0) [ft] off from the geometrical centre (keep the mass moments of inertia at the centre of mass as is). Change the model and simulate the same driving motion. Plot the container's angular rotation around its vertical axle as a function of time and compare this result with the symmetrical situation. Is there a significant difference such that positioning of the container on the AGV will give trouble? Explain!



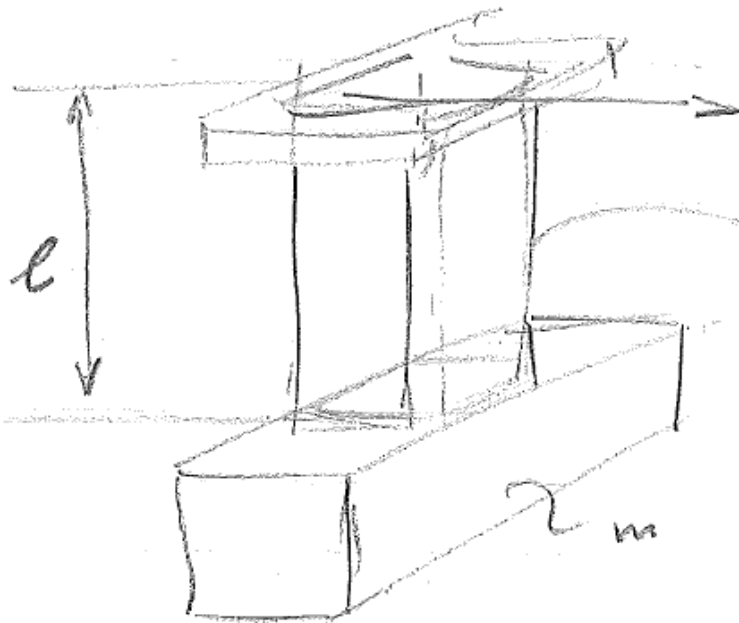
# Assignment 3

De contactruimte

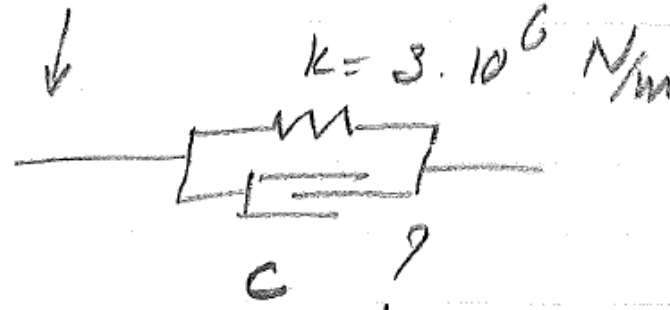


Welke kant op bewegen?

ft  
TON  
m  
m/m

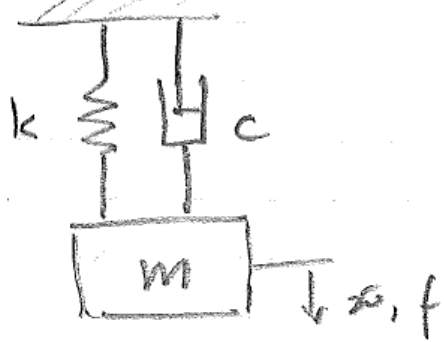


veer-dempen element



Material Demping  $\pm 5\%$  (van Duit)  
 De bedoelde relatieve demping  $\beta = 0.05$





$$m \ddot{x} + c \dot{x} + k x = f$$

$$\ddot{x} + \frac{c}{m} \dot{x} + \frac{k}{m} x = 0 \quad \text{gevel.}$$

$$\ddot{x} + 2\beta\omega_0 \dot{x} + \omega_0^2 x = 0$$

$$\omega_0 = \sqrt{\frac{k}{m}} \quad \text{eigenfrequentie}$$

$$\beta = \frac{c}{2m\omega_0} \quad \text{relatieve demping}$$

$\beta > 1$  Overgedempt

Overdamping

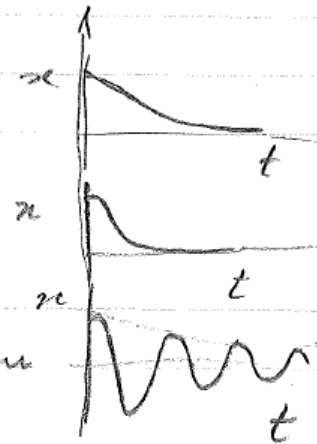
$\beta = 1$  Kritisch gedempt

Critical Damping

$\beta < 1$  Ondergedempt

Under Damping

Oscillating Amplitude



Zie Meridian & Kraay H 8

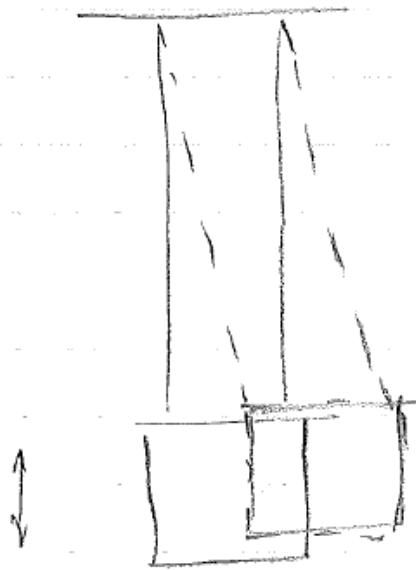
$$\omega_n = \sqrt{1 - \beta^2} \omega_0 \quad x = x_0 e^{-\beta\omega_0 t} \cdot \cos(\omega_n t + \phi_0)$$

Welke wa er zijn er zo veel?



Hoeveel de langst deze dampen  
ziet op beweging afweg zeker  
sterker weten

Wat is de langste?



$$m = \frac{32500}{30000} \text{ kg} \quad k = 4 * 3 \cdot 10^6$$

$$\beta = 0.05 \quad c = 0.1 \cdot \frac{32500}{30000} \sqrt{\frac{4 \cdot 3 \cdot 10^6}{32500}}$$

$$c = 0.1 \sqrt{\frac{4 \cdot 3 \cdot 10^6 \cdot 3 \cdot 10^4}{3.25 \cdot 10^9}} \approx 0.1 \cdot 2 \cdot 3 \cdot 10^5 = 6 \cdot 10^4$$

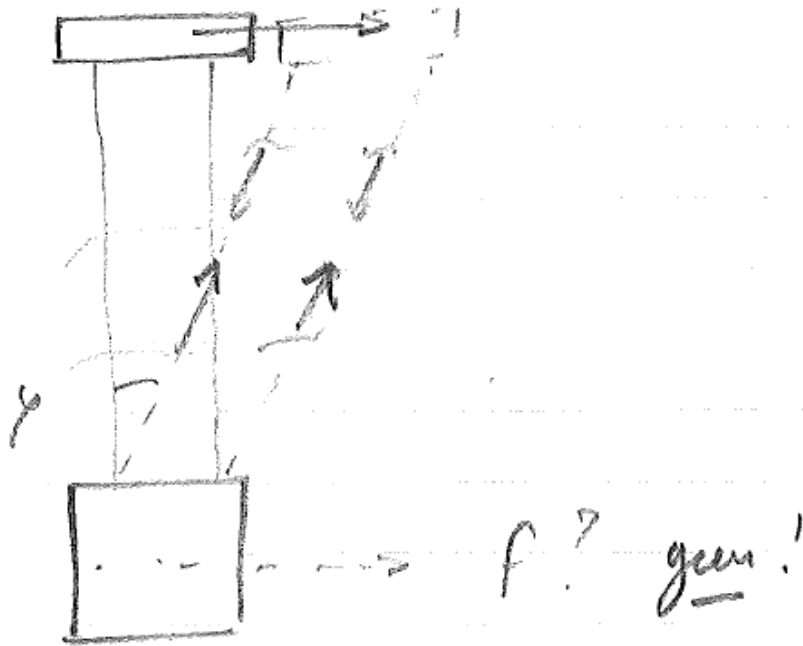
$$1 \text{ veer } \frac{c}{4} = 1.5 \cdot 10^4 \text{ [Ns/m]}$$

Dat is De T van de lastslingering?

Dat is zelf nu over nu

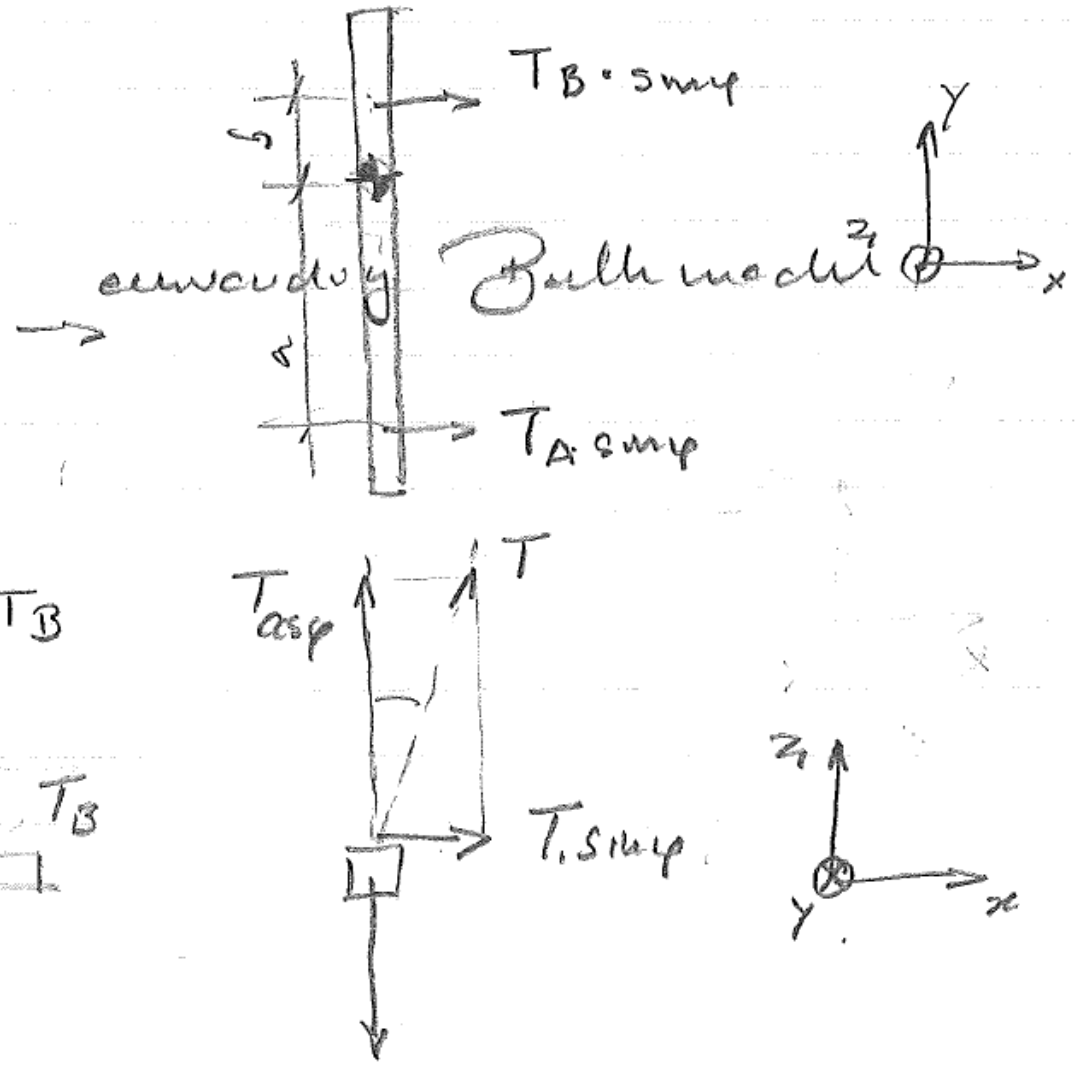
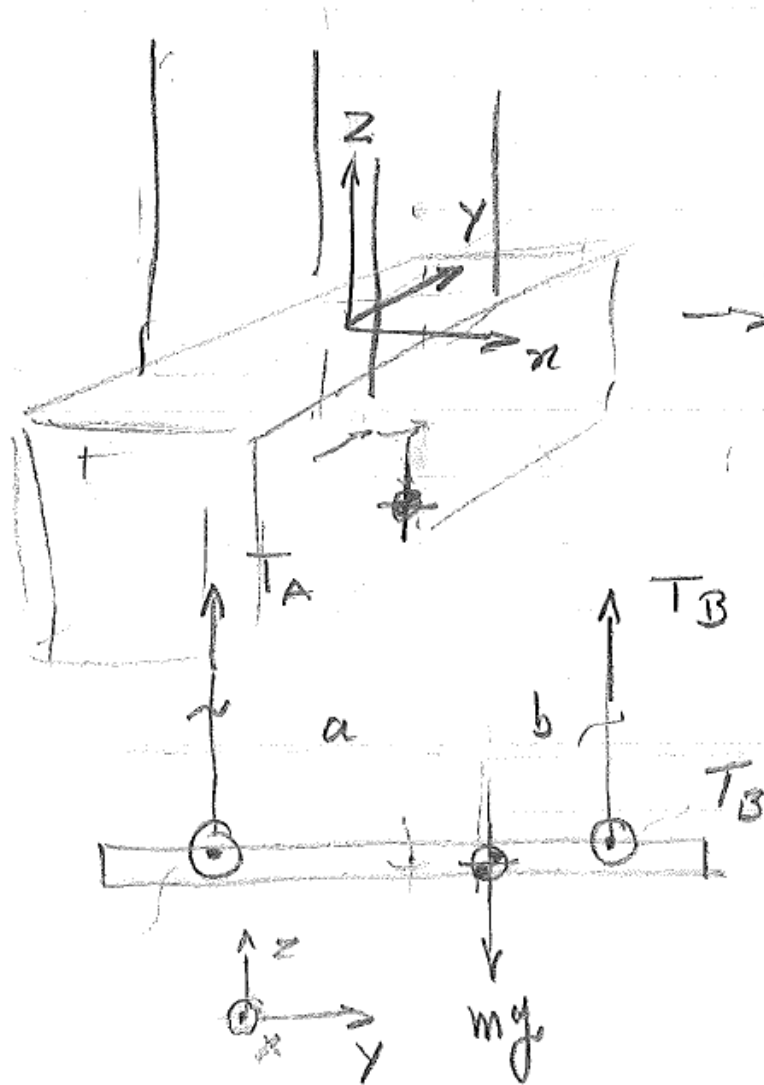
Wellicht kan ADAMS je wel antwoorden geven

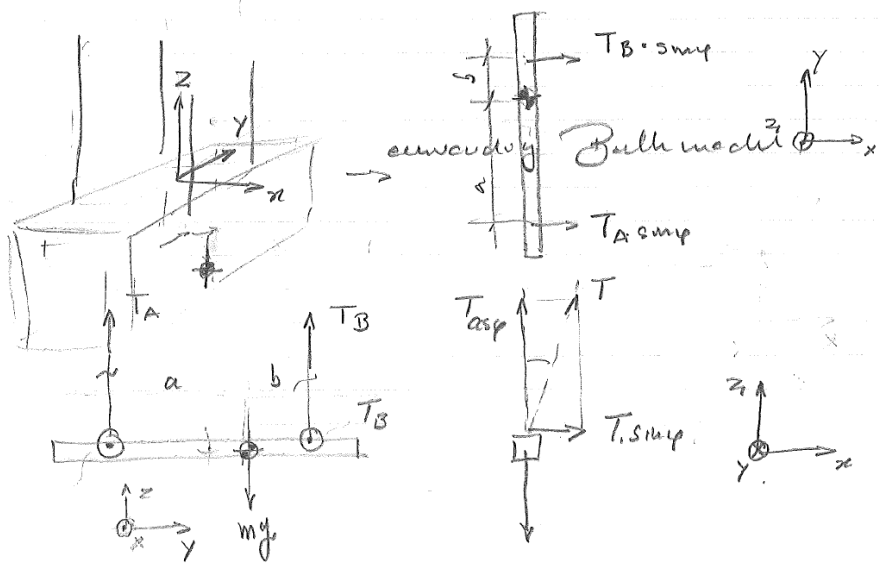
Waarom gaat de Cartainu Zwager?



$$f = F_{\text{vert}} \cdot \sin \gamma$$

Stetvraag belastingen  
 Zet de centrale of A-sym  
 gem. Stijfheid?





Massa middelpunt

$$\sum F_x = m \ddot{x}$$

$$\sum F_y = m \ddot{y}$$

$$\sum F_z = m \ddot{z}$$

$$T_A \cdot \sin \varphi + T_B \cdot \sin \varphi = m \ddot{z}$$

$$0 = m \ddot{y}$$

$$T_A \cdot \cos \varphi + T_B \cdot \cos \varphi - mg = m \ddot{z}$$

$$\sum M_x = J_{xx} \ddot{\omega}_x \quad -T_A \cos \varphi \cdot a + T_B \cos \varphi \cdot b = I_{xx} \ddot{\omega}_x$$

$$\sum M_y = J_{yy} \ddot{\omega}_y \quad 0 = I_{yy} \ddot{\omega}_y$$

$$\sum M_z = J_{zz} \ddot{\omega}_z \quad T_A \sin \varphi \cdot a - T_B \sin \varphi \cdot b = I_{zz} \ddot{\omega}_z$$

8 Onbekende 6 Vergelijking?

2 Veerbettingsvoorwaarden  $l_{1,2} = \text{const}$   $\rightarrow \ddot{z} = 0$   
 $\ddot{\omega}_x = 0$

$$T_A + T_B = \frac{mg}{\cos \varphi}$$

$$-T_A \cos \varphi \cdot a + T_B \cos \varphi \cdot b = 0$$

$$T_B = \frac{a}{b} T_A$$

$$\left(1 + \frac{a}{b}\right) T_A = \frac{mg}{\cos \varphi}$$

$$T_A = \frac{b}{a+b} \cdot \frac{mg}{\cos \varphi}$$

$$T_B = \frac{a}{a+b} \cdot \frac{mg}{\cos \varphi}$$

$$\ddot{z} = -g \cdot \tan \varphi \quad \varphi \ll 1$$

$$\ddot{z} \approx -g \cdot \varphi$$

$$\ddot{y} = 0$$

$$\ddot{\omega}_y = 0$$

$$\ddot{\omega}_z = ? \quad \varphi$$